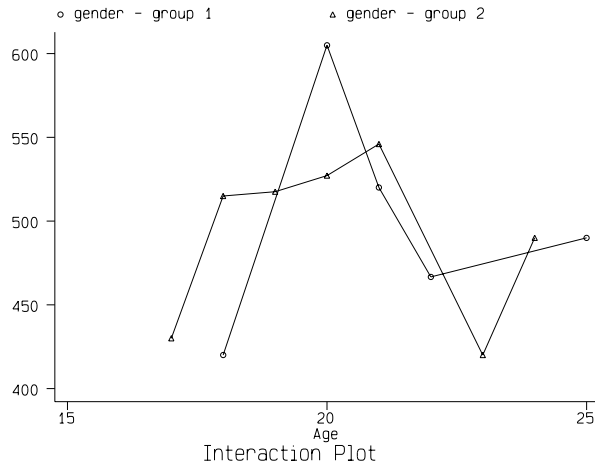


STAT302: Secs 102 & 103  
Summer I 1999  
Exam #4  
**Form A**

Instructor: Julie Hagen Carroll

1. **Don't even open this until you are told to do so.**
2. Be sure to mark your section number (102 or 103) and your test form (A, B, C or D) on the scantron!
3. Sign your name where indicated on your scantron and write your Wednesday section number and computer number beside it.
4. There are 20 multiple-choice questions on this exam, each worth 5 points. There is partial credit. Please mark your answers **clearly** on the scantron. Multiple marks will be counted wrong.
5. You will have 60 minutes to finish this exam.
6. If you are caught cheating or helping someone to cheat on this exam, you both will receive a grade of **zero** on the exam. You must work alone.
7. This exam is worth 100 points, and will constitute 20% of your final grade.
8. Good luck!

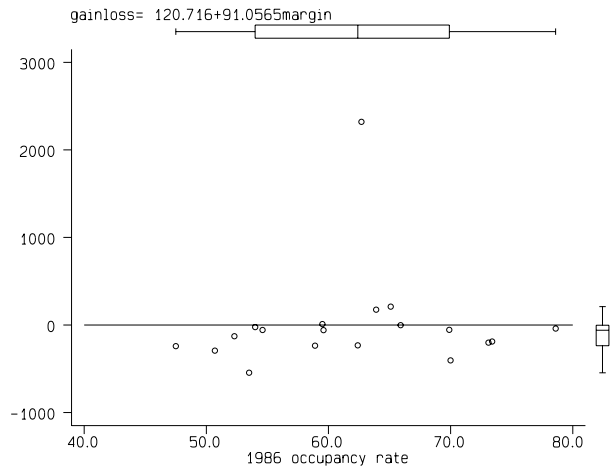


- What conclusions may be drawn from the interaction plot above?
  - The lines cross, therefore, there is significant interaction between *Age* and *Gender*.
  - The lines cross, therefore, there is NOT significant interaction between *Age* and *Gender*.
  - The lines cross, therefore, *Age* and *Gender* have a significant effect.
  - The lines cross, therefore, *Gender* has a significant effect.
  - The lines cross, therefore, *Age* has a significant effect.

Source	Partial SS	df	MS	F	Prob > F
gend	1.008638264	1	.008638264	0.03	0.8753
age	13.36985862	10	.336985862	0.98	0.4825
gend*age	2.42676946	2	1.21338473	3.52	0.0427
Residual	9.98636364	29	.344357367		
Total	14.7906977	42	.352159468		

- (NOTE: this output is NOT related to the graph above, so don't let it affect your answer to that question.) We must assume that the variance is constant within each *Age* and *Gender* combination (they are all equal) for the *F*-tests to be valid. What is our estimate of this variance?
  - We need a residual plot to tell if it is safe to assume that the variance is constant.
  - 1.213
  - 0.344
  - 0.352
  - 3.52
- What is the best conclusion based on the output above?

- The  $p$ -value = 0.0427, so we cannot assume that the variances are equal.
- The  $p$ -value = 0.0427, so we can assume that the variances are equal.
- The  $p$ -value = 0.0427, so we can *Age* and *Gender* are significant effects.
- The  $p$ -value = 0.0427, so we can *Age* and *Gender* are NOT significant effects.
- The  $p$ -value = 0.0427, so we can the interaction between *Age* and *Gender* is significant.



- What does the residual plot above indicate?
  - The assumption of equal variances (constant) has been violated.
  - The assumption of normality may have been violated.
  - The assumption of all points being equally weighted has been violated.
  - The assumption of linearity has been violated.
  - All of the assumptions for simple linear regression are valid.
- Why do we use  $\alpha = 0.10$  for the Barlett's test of equal variances?
  - We want to increase the chance of a Type I error.
  - We want to reduce the chance of a Type I error.
  - We want the  $p$ -value for the *F*-test to be smaller.
  - We want to be sure we are doing a valid procedure.
  - We want to be sure that the means are equal.

Source	SS	df	MS
Model	47.5154184	1	47.5154184
Residual	8.0485833	8	1.00607291
Total	55.5640017	9	6.17377797

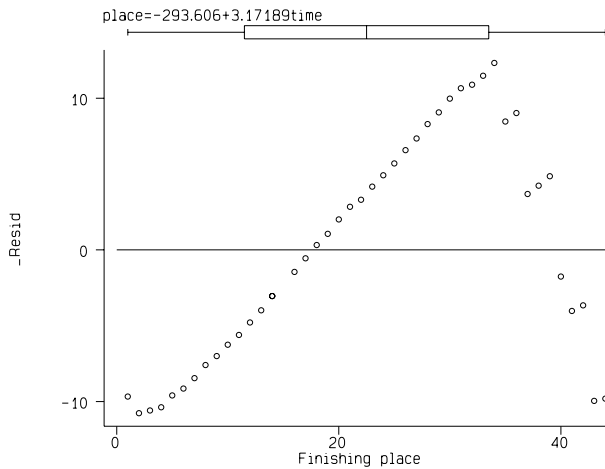
fertile	Coef.	Std. Err.	t	P> t	[95%ConfInt]
fschool	-.06872	.009998	-6.872	0.000	-.0918 -.0456
_cons	7.3465	.528655	13.897	0.000	6.1274 8.566

6. According to the output above, is *fschool*, the percent of females enrolled in secondary schools, a viable means of predicting the fertility rate, *fertile*?
- Of course, the more educated the population, the lower the risk of unwanted pregnancies.
  - The  $p$ -value = 0.000, so the true slope,  $\beta_1 = 0$ .
  - The  $p$ -value = 0.000, so yes, we should use *fschool* to predict *fertile* rather than just the average fertility rate.
  - The sample slope,  $b_1 = -0.06872$ , which is practically 0, so no, we shouldn't use *fschool* to predict *fertile*.
  - The sample slope,  $b_1 = -0.06872$ , which is not 0, so, we should use *fschool* to predict *fertile*.
7. What is the correlation coefficient,  $r$ , for the output above?
- 0.06872
  - 0.06872
  - 0.2604
  - 0.9247
  - 0.9247
8. Again using the output above, what is the total variance of *fertile*, the fertility rate?
- 47.515
  - 8.0486
  - 55.564
  - 1.0061
  - 6.1738

Spouse abuse present marriage	Present family type			Total
	intact	remarry	reconst.	
no abuse	743	92	78	913
abuse	36	9	11	56
Total	779	101	89	969

Pearson chi2(2) = 10.8147 Pr = 0.004

9. Using the Two-way table above, which represents the counts of families with or without spousal abuse by the type of family, would you say the two categories are independent?
- It is obvious *family type* and *spousal abuse* are related, since 'broken' families tend to be more violent.
  - It is obvious *family type* and *spousal abuse* are related, since families tend split because of violence.
  - The  $p$ -value for testing whether *family type* and *spousal abuse* are related is 0.004, so there is only a 0.4% chance that the two are related.
  - The  $p$ -value for testing whether *family type* and *spousal abuse* are related is 0.004, so the hypothesis that the two are independent would be rejected.
  - The  $p$ -value for testing whether the variances are equal is 0.004, so the assumption of equal variances is invalid.
10. What is the probability of being in a *remarried* and *abusive* family if the two categories are independent?
- 9/969
  - 101/969 \* 56/969
  - (101\*56)/969
  - 9/101
  - 9/56
11. What does it mean to be 'statistically significant'?
- It means that you rejected the null hypothesis.
  - It means that you found the means to be significant.
  - It means there really is some reason to do a hypothesis test.
  - It means there is an influential point in the data.
  - It means that you passed STAT302.



12. What does the plot above tell us?

- A. The relationship between *Finishing place* and *time* is not strictly linear.
- B. The relationship between the residuals and *time* is not strictly linear.
- C. The residuals are not strictly linear.
- D. The residuals don't have constant variance.
- E. The residuals are skewed, therefore, not normally distributed.

Variable	Obs	Mean	Std. Dev.
age	13	3.753846	1.637893
estage	13	3.861538	1.823247
diff.	13	-.1076923	.9059631

Ho: mean difference = 0 (paired data)  
 t = -0.43 with 12 d.f.  
 Pr > |t| = 0.6758  
 95% CI for difference = (-.65516029, .43977571)

13. The above output is a paired *t*-test for testing whether there is a difference in the true *age* and the *estimated age*. The *p*-value = 0.6758. Had we done a two-sample *t*-test instead, would we still have found no difference in the ages?

- A. Yes, the paired *t*-test has the most power, so if it couldn't find a difference, neither could a two-sample *t*.
- B. It makes no sense to NOT do a paired *t*-test, since we're comparing how good the estimates are.
- C. The *p*-value would be larger for the two-sample *t*, so it would be even harder to get a rejection.
- D. All of the above are correct.
- E. Exactly two of the above are correct (excluding D.).

Political party preference	Summary of Mathematics SAT score		
	Mean	Std. Dev.	Freq.
Democrat	512.85714	93.102803	14
Republic	538.57143	55.205245	7
Independ	492.14286	60.533344	14
Total	509.71429	74.537228	35

Source	Analysis of Variance				
	SS	df	MS	F	Prob > F
Between	10290.00	2	5145.00	0.92	0.4081
Within	178607.143	32	5581.473		
Total	188897.143	34	5555.798		

Bartlett's test for equal variances:  
 chi2(2) = 3.2232 Prob>chi2 = 0.200

14. Does one's *Political party preference* affect the true mean Math SAT score?

- A. Yes, the *p*-value is 0.20, so we reject the null and conclude that there is a difference in the means.
- B. No, the *p*-value is 0.20, so we fail to reject the null and conclude that there is not a difference in the means.
- C. No, the *p*-value is 0.4081, so we fail to reject the null and conclude that there is not a difference in the means.
- D. Yes, the *p*-value is 0.4081, so we reject the null and conclude that there is a difference in the means.
- E. No, the *p*-value is 0.92, so we fail to reject the null and conclude that there is not a difference in the means.

15. What is the correct alternative hypothesis for the output above?

- A.  $H_0 : \mu_D = \mu_R = \mu_I$
- B.  $H_A : \mu_D = \mu_R = \mu_I$
- C.  $H_A : \mu_D \neq \mu_R \neq \mu_I$
- D.  $H_A$ : all of the means are not the same
- E.  $H_0$ : all of the means are the same

16. What is the consequences of making a Type I error in One-way ANOVA?
- A. You conclude that the variances are equal, but they really aren't so you use an invalid  $F$ -test.
  - B. You conclude that there is an effect due to the different groups, but there really is not.
  - C. You conclude that the variances are not all equal, but they really are different.
  - D. You conclude that the means are equal when they really are not.
  - E. Exactly two of the above are Type I errors.

```

Number of obs =      11
F( 1,      9) =  21.27
Prob > F      =  0.0013
R-squared     =  0.7027
Adj R-squared =  0.6696
Root MSE     =  38.873
    
```

Source	SS	df	MS
Model	32140.9628	1	32140.9628
Residual	13599.7645	9	1511.08495
Total	45740.7273	10	4574.07273

	Coef.	Std.Err.	t	P> t	[95% Conf. Int]
vsat	1.0351	.2244	4.612	0.001	.5274 1.543
_cons	12.1834	123.77	0.098	0.924	-267.81 292.18

17. If the point (400,326) were added to the model above which of the following would happen?
- A. The  $R^2$  would decrease and the standard deviation of the regression line,  $s_e$ , would increase.
  - B. The  $R^2$  would increase and the standard deviation of the regression line,  $s_e$ , would decrease.
  - C. The  $R^2$  would decrease and the standard deviation of the regression line,  $s_e$ , would decrease.
  - D. The  $R^2$  would increase and the standard deviation of the regression line,  $s_e$ , would increase.
  - E. Neither  $R^2$  nor  $s_e$  would change.
18. If instead of adding a point, we decided to multiply the Math SAT scores,  $msat$ , by 100, which of the following would happen?
- A. Nothing would change since you haven't actually changed the relationship.

- B. The  $R^2$  and  $s_e$  would both increase by a factor of 100.
- C. The  $s_e$  would increase by a factor of 100.
- D. The  $R^2$  would increase by a factor of 100.
- E. The  $R^2$  would decrease by a factor of 100.

Sex	Mean	Std. Dev.	Freq.
male	4.5833334	1.9772878	6
female	3.0428571	.91078198	7
Total	3.7538462	1.6378927	13

Source	SS	df	MS	F	Prob > F
Between	7.66683197	1	7.66683	3.44	0.0907
Within	24.5254776	11	2.22959		
Total	32.1923095	12	2.682692		

Bartlett's test for equal variances:  
 $\chi^2(1) = 2.8612$  Prob> $\chi^2 = 0.091$

19. What is the correct conclusion for the output above?
- A. The  $p$ -value for Bartlett's test is less than the  $p$ -value for the  $F$ -test, so we reject the null hypothesis.
  - B. The  $p$ -value for Bartlett's test is not greater than 10%, so we conclude we cannot say the variances are equal.
  - C. The  $p$ -value for Bartlett's test is not greater than 10%, so we fail to reject and conclude the variances are equal.
  - D. The  $p$ -value for  $F$ -test is not greater than 10%, so we fail to reject and conclude the variances are equal.
  - E. The  $p$ -value for  $F$ -test is not greater than 10%, so we fail to reject and conclude the means are equal.
20. How much of the total variation of *actual age* was explained by the difference in the sexes?
- A. 7.667/24.525
  - B. 7.667/2.230
  - C. 7.667/32.192
  - D. 7.667/2.683
  - E. 2.230/2.683

1A,2C,3E,4B,5D,6C,7E,8E,9D,10B,11A,  
 12A,13D,14C,15D,16B,17A,18C,19B,20C